

$$\{|n\rangle\}_{n \in \mathbb{N}}$$

**Structura/FUNCTIILE de BAZA (STARI SELECTATE – FUNDAMENTALE/ELEMENTARE)**

In spatiul (TUTOROR) starilor  
De existenta a nivelurilor  
(energetice) de existenta  
a electronilor in sisteme  
Multielectronice (chimice)  
& UNITATEA DE UNIVERS “1”

$$\hat{1} = \sum_n |n\rangle\langle n|$$

“Macro”

“Micro/nano”

$$\langle \hat{A} \rangle_k = \frac{\langle \varphi_k | \hat{A} | \varphi_k \rangle}{\langle \varphi_k | \varphi_k \rangle} = \frac{\sum_{n,n'} \langle \varphi_k | n' \rangle \langle n' | \hat{A} | n \rangle \langle n | \varphi_k \rangle}{\sum_n \langle \varphi_k | n \rangle \langle n | \varphi_k \rangle} = \frac{\sum_{n,n'} c_{kn} c_{kn'}^* \langle n' | \hat{A} | n \rangle}{\sum_n |c_{kn}|^2}$$

“Fundamental/Universal”  
 (“sub-nanosopic”)

$$|\varphi_k\rangle = \sum_n c_{kn} |n\rangle$$

REPREZENTARE “ORBITALA”  
(a electronului) prin “punctele”  
Sale de reprezentare fundamentala /n>!

MEDIA OBSERBABILEI “A” = <observabila in stare masurata pe starea “k”> /  
pe starea “k” <starea ne-masurata, libera, “k”>

“ELECTRONII” reprezentati prin functiile lor de BAZA  
(=functiile de unda ale electronilor – PHI  
se reprezinta prin (ISTORIA DE) functii de unda  
“mai” fundamentale)

De ce?

ELECTRONULUI – ca PARTICULA FUNDAMENTALA a materiei  
(ne spun Experimentele, si istoria stintelor naturii)

...ii asociem o stare...o functie de unda- PHI(k)!

/n> - functii de unda FUNDAMENTALE pentru starile electronilor  
(asa cum ne invata mecanica cuantica)

AVANTAJUL ABORDARII: Toti electronii din sistem se vor reprezenta

(in structura, dinamica, proprietati) PRIN ACELASI SET DE STARI/VETORI/FUNCTII DE baza {/n>}

$$\langle \hat{A} \rangle = \frac{\sum_k w_k \langle A \rangle_k}{\sum_k w_k}$$

$$\langle \hat{A} \rangle = \frac{\sum_{n,n'} \langle n | \hat{\rho} | n' \rangle \langle n' | \hat{A} | n \rangle}{\sum_k w_k}$$

Reprezentarea DENSITATII ELECTRONICE (cu toate interactiile inter-electronice incluse)  
pe FUNCTIILE DE BAZA “n”

$$\langle n | \hat{\rho} | n' \rangle = \sum_k w_k \frac{c_{kn} c_{kn'}^*}{\sum_k |c_{kn}|^2}$$

**= MATRICEA DENSITATE!**  
(in reprezentarea functiilor electronice)!

$$\hat{\rho} = \sum_{n,n'} |n\rangle\langle n | \hat{\rho} | n' \rangle \langle n'| = \sum_k \frac{w_k}{\sum_n |c_{kn}|^2} \left( \sum_n c_{kn} |n\rangle \right) \left( \sum_{n'} \langle n' | c_{kn'}^* \right) = \sum_k \frac{w_k}{\sum_n |c_{kn}|^2} |\varphi_k\rangle\langle \varphi_k|$$

$$\langle \varphi_k | \hat{\rho} | \varphi_k \rangle = w_k$$

**= MATRICEA DENSITATE**  
(in reprezentarea functiilor electronice)!

CHIMIA  
=Fizica (structura si dinamica materiei)  
sistemelor multielectronice

Handwritten notes on a chalkboard regarding quantum chemistry and density matrix approach.

$\langle m | \psi \rangle = \sum_k c_k \langle m | \psi_k \rangle$   
 $\langle m | \psi \rangle = \sum_k c_k \langle m | \psi_k \rangle = \langle \psi | \psi \rangle = \sum_k c_k \langle m | \psi_k \rangle \sum_k c_k \langle m | \psi_k \rangle = \sum_k c_k^2 \langle m | \psi_k \rangle \langle m | \psi_k \rangle = \sum_k c_k^2$

$\hat{I} = \sum_k | \psi_k \rangle \langle \psi_k |$   
 $\langle \psi | \hat{I} | \psi \rangle = \langle \psi | \psi \rangle = 1$

$\langle \psi | \hat{A} | \psi \rangle = \sum_k \langle \psi | \psi_k \rangle \langle \psi_k | \hat{A} | \psi \rangle = \sum_k c_k \langle \psi | \psi_k \rangle \langle \psi_k | \hat{A} | \psi \rangle$

$\hat{A} (n \times n) = \begin{pmatrix} \langle \psi_1 | \hat{A} | \psi_1 \rangle & \dots \\ \langle \psi_2 | \hat{A} | \psi_1 \rangle & \dots \end{pmatrix}$

Additional notes and diagrams:
 

- Diagram showing a state  $|\psi\rangle = \sum_k c_k |\psi_k\rangle$  and its components.
- Diagram showing the identity operator  $\hat{I} = \sum_k |\psi_k\rangle \langle \psi_k|$ .
- Diagram showing the expectation value of  $\hat{A}$  as a trace of a product of matrices.
- Diagram showing the density matrix  $\rho = \sum_k c_k |\psi_k\rangle \langle \psi_k|$ .
- Diagram showing the expectation value of  $\hat{A}$  as  $\text{Tr}(\hat{A} \rho)$ .
- Diagram showing the matrix elements of  $\hat{A}$  and  $\rho$ .